

# Boolean Algebra (Mathematical Logic) for Computational Differential Diagnosis in Medicine

**Gerhard Zugmaier**

Department of Haematology, Oncology and Immunology, Philipps University Marburg, Marburg, Germany.

**\*Corresponding Author:** Gerhard Zugmaier, MD, Department of Haematology, Oncology and Immunology, Philipps University Marburg, Marburg, Germany.**Received date:** November 18, 2024; **Accepted date:** January 05, 2025; **Published date:** January 13, 2025**Citation:** Gerhard Zugmaier, (2024), Boolean Algebra (Mathematical Logic) for computational Differential Diagnosis in Medicine, *J Clinical Research and Reports*, 18(1); DOI:10.31579/2690-1919/439**Copyright:** © 2024, Gerhard Zugmaier. This is an open access article distributed under the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

## Abstract

**Background:** Medical diagnosis has become challenging due to the complexity of disease definition. An arsenal of methods is necessary to conduct a correct differential diagnosis**Aim:** This study used computational medicine in form of Boolean algebra to assess diagnosis. We used Boolean algebra as rigid framework designed to aid in differential diagnosis.**Results:** Each symptom or test result was represented as a Boolean variable. Each condition or disease was represented as a Boolean variable.**Conclusion:** Boolean algebra can be used to model and simplify decision-making processes in differential diagnosis.**Keywords:** Boolean Algebra; differential diagnosis; clinical symptoms and signs; medicine

## Introduction

Precise diagnosis is essential for successful treatment. It enables exact definition of disease and patient-adapted treatment. Precise and swift diagnosis is an essential-condition for successful handling of patients with any disease. The international statistical classification of diseases and related health problems (ICD) from the World Health Organization (WHO) has established a defined process of disease definition [3]. Although numerous advanced technologies for diagnosis have become available [15,16,1,3], clinical symptoms and signs are still the essentials of any differential diagnostic process. Boolean algebra provides a rigorous framework for designing and optimizing diagnostic systems, ensuring consistency and efficiency. As shown previously [20-24]. In this study we set out to use Boolean algebra as part of computational medicine for differential diagnosis based on clinical symptoms and signs as shown previously for definition of disease and for abnormal laboratory values [20-24].

## Materials and Methods

Symbols of Boolean Algebra

1. Variables:

o Each Boolean variable can take one of the values 1 or 0.

2. Operations:

o AND:

- $A \cdot B$  or  $A \wedge B$
- The result is 1 if both A and B are 1; otherwise, it is 0.
- Example:  $1 \cdot 1 = 1$ ,  $1 \cdot 0 = 0$

o Inclusive OR:

- $A + B$  or  $A \vee B$
- The result is 1, if A or B or both are 1; if both are 0, the result is 0.
- Example:  $1 + 0 = 1$ ,  $0 + 0 = 0$

o NOT:

- $\neg A$
- The result is the inverse of A; if A is 1,  $\neg A$  is 0, and vice versa.
- Example:  $\neg 1 = 0$ ,  $\neg 0 = 1$

o XOR:

- $A \oplus B$
- The result is 1, if exactly one of A or B is 1, but not both. It is also 0, if both A and B are 0.

Example:  $1 \oplus 0 = 1$ ,  $1 \oplus 1 = 0$ 

o XNOR:

- $A = B$
- The result is 1 if A and B are both 1 or both 0.
- Example:  $1 = 1$ ,  $0 = 0$

"if A, then B" is: expressed as  $A \rightarrow B = \neg A \vee B$ . The arithmetic rules of the inclusive OR are applied.

In the formulas the following operators take precedence:

- $()$  over each operator
- $\neg$  over  $\wedge$
- $\wedge$  over  $\vee$ ,

$\vee$ ,  $\oplus$  over  $=$ <sup>17</sup>

Examples of multiple Representations for the Same Operations<sup>7</sup>:

AND:

$A \cdot B$  or  $AB$ : Common in traditional Boolean algebra and engineering

$A \wedge B$ : Used in formal logic and computer science

$A$  AND  $B$  Seen in programming pseudocode or textual descriptions

OR (Inclusive OR):

$A + B$ : Traditional Boolean algebra

$A \vee B$ : Used in logic and theoretical fields

$A$  OR  $B$ : Common in programming and textual representations

XOR (Exclusive OR):

$A \oplus B$ : Theoretical computer science and mathematics

$A$  XOR  $B$ : Textual or programming contexts

## Results

In this section clinical symptoms and signs are listed with the combinations of clinical symptoms and signs leading to the correct diagnosis. The symbols are explained in Materials and Methods. The major clinical signs or clinical symptoms are listed in alphabetical order.

Bell's palsy  $\rightarrow$  herpes simplex 1

Blood pressure  $\downarrow$   $\wedge$  normal pulse  $\rightarrow$  autonomic insufficiency

Delirium  $\rightarrow$  metabolic encephalopathy

Epitrochlear lymph nodes palpable  $\rightarrow$  infections forearm  $\vee$  lymphoma  $\vee$  sarcoidosis  $\vee$  tularemia  $\vee$  syphilis

Fever  $> 38\text{ C}$   $\wedge$  tachycardia  $\wedge$  hypertension  $\wedge$  delirium  $\wedge$  rigidity  $\wedge$   $\neg$  clonus  $\rightarrow$  neuroleptic malignant syndrome

Fever  $> 38\text{ C}$   $\wedge$  tachycardia  $\wedge$  hypertension  $\wedge$  delirium  $\wedge$  rigidity  $\wedge$  clonus  $\rightarrow$  serotonin syndrome

Further from equator  $\wedge$  optic neuritis  $\rightarrow$  multiple sclerosis

Herpes zoster ad nose  $\rightarrow$  corneal herpes zoster

Indolent lymph nodes  $\wedge$  advanced age  $\uparrow$   $\wedge$  smoker  $\rightarrow$  head and neck cancer

Lemiere's syndrome (septic thrombophlebitis of vena jugularis interna)  $\rightarrow$  septic pulmonary emboli

Lymph nodes  $\uparrow$   $\wedge$  spleen  $\uparrow$   $\rightarrow$  lymphoma  $\vee$  lymphatic leukemia  $\vee$  mononucleosis

Nephrotic syndrome  $\rightarrow$  risk  $\uparrow$  of venous thrombosis

Osler lesions  $\rightarrow$  immune complex nephritis

Painless jaundice  $\rightarrow$  cancer pancreas head

Paroxysmal nocturnal hemoglobinuria  $\rightarrow$  iron  $\downarrow$

Postprandial blood pressure  $\downarrow$   $\wedge$  reversal of circadian pattern  $\rightarrow$  orthostatic hypotension

Pulsus paradoxus  $\rightarrow$  cardiac tamponade  $\vee$  pericarditis constrictiva  $\vee$  chronic obstructive pulmonary disease  $\vee$  asthma

Recurrent aphthous ulcers  $\rightarrow$  Behcet's  $\vee$  Crohn's disease

Sudden thoracal pain  $\rightarrow$  pneumothorax

Unilateral right varicocele  $\rightarrow$  obstruction of vena cava inferior

Widened pulse pressure  $\rightarrow$  persistent ductus arteriosus

## Discussion:

We have applied Boolean Algebra to differential diagnosis of clinical symptoms and signs. The clinical symptoms and signs were used in this study as described in Suneja et al. [4] Boolean algebra is part of computational medicine to calculate complex permutations. It includes a number system with the sole integers 0 and 1. Boolean arithmetic has been defined by Shannon [13]. In Boolean arithmetic  $1 + 1 = 1$  is correct. Other than the rules of addition apply.

In this study, we applied Boolean operations to standardize differential diagnosis based on clinical symptoms and signs.

Mathematics is indispensable in medicine, serving as a bridge between theoretical concepts and practical applications. It enables precise modeling, efficient computation, and improved patient outcomes, transforming the landscape of healthcare and biomedical research [9].

Boolean algebra has significant applications in computational medicine, where binary systems play a crucial role in modeling, analyzing, and solving medical problems. It is particularly effective in areas requiring clear decision-making, rule-based systems, and systematic modeling of biological or medical data. IT is foundational in developing decision-support systems that assist healthcare professionals in diagnosing and treating diseases [2, 8, 18, 5, 11, 10, 20-24]

The term "mathematical logic" is used in a strict mathematical context. It should not be confused with logic as basis of any scientific inquiry [6,14].

The lack of standardization in mathematical symbols can cause confusion, miscommunication, and inefficiencies in education, research, and communication. This issue stems from historical, cultural, and contextual differences in how symbols are used and interpreted across disciplines, regions, and even individuals [19]).

Boolean algebra's confusing notation arises from the diversity of its applications across mathematics, computer science, engineering, and mathematical proof theory. Each field often adopts conventions that suit its specific needs, leading to multiple ways to express the same operations<sup>7</sup>.

This study has various limitations. Boolean algebra, while useful for modeling logical systems and binary decision-making processes, has significant limitations when applied to differential diagnosis in complex medical or problem-solving contexts. These limitations arise due to the inherent oversimplification in mathematical logic, which may not adequately reflect the nuanced realities of medical decision-making. Boolean algebra cannot incorporate probabilities or degrees of uncertainty, which are crucial in medical diagnosis. Differential diagnosis often relies on Bayesian reasoning or probabilistic methods or both, which Boolean algebra does not support. Machine learning-based methods, which can learn from historical patient data, are more effective in modern diagnostic tools. Bayesian reasoning, probabilistic methods and Boolean algebra are not mutually exclusive but complement each other, since all 3 methods have advantages and limitations. The pros and cons of the 3 methods are detailed in Table 1.

Feature	Boolean Algebra	Probabilistic Models	Machine Learning Models
Binary or Continuous Data	Binary only	Handles probabilities, continuous data	Handles both and abstract patterns
Handles Uncertainty	No	Yes	Yes
Learns from Data	No	Limited	Yes
Temporal Reasoning	No	Limited	Yes (e.g., recurrent neural networks)
Incorporates Interdependencies	Limited	Yes	Yes

**Table 1:** Comparison to Probabilistic and Machine Learning Models

## Conclusion

Boolean algebra has a role in structured, rule-based diagnostic systems but falls short in addressing the complexities of real-world differential diagnosis. Probabilistic reasoning, machine learning, and temporal modeling offer more robust solutions for modern medical diagnostic challenges. Boolean models are best used in conjunction with these advanced tools rather than as standalone systems.

## References

- Alaggio, R., Amador, C., Anagnostopoulos, I. et al. (2022). The 5th edition of the World Health Organization Classification of Haematolymphoid Tumours: Lymphoid Neoplasms. *Leukemia* 36, 1720–1748.
- Albert R, Robeva R. (2015). Signaling Networks: Asynchronous Boolean Models. *Algebraic and Discrete Mathematical Methods for Modern Biology*: 65-91.
- Cazzola M, Sehn LH. (2022) Developing a classification of hematologic neoplasms in the era of precision medicine. *Blood*. 15;140(11):1193-1199.
- De Gowin's Diagnostic Examination. M. Suneja M, Szot JF, LeBlond RF, Brown D. (2020) 11th Edition, McGraw, Hill,
- DiAndreth B, Hamburger AE, Xu H, Kamb A. (2022). The TMOD Cellular Logic Gate as a Solution for Tumor-Selective Immunotherapy. *Clinical Immunology*. 241: 1-8.
- Grattan-Guinness I. (1999). Mathematics and Symbolic Logics: Some Notes on an Uneasy Relationship. *History and Philosophy of Logic*. 20(3-4):159-167.
- Hoffmann DW. (2016). *Grundlagen der technischen Informatik*. 5. Auflage. München: Carl Hanser Verlag.
- Macauley M, Young N. (2020). The Case for Algebraic Biology: From Research to Education. *Bulletin of Mathematical Biology*. 82(9):115. doi:10.1007/s11538-020-00789-w
- Matthäus F, Matthäus S, Harris S, Hillen T. (2020). *The Art of Theoretical Biology*. Springer.10.
- Palma A, Iannuccelli M, Rozzo I, (2021) et al. Integrating Patient-Specific Information into Logic Models of Complex Diseases: Application to Acute Myeloid Leukemia. *Journal of Personalized Medicine*. 11(2):117.
- Riede U, Moore GW, Williams MB (1983). Quantitative Pathology by Means of Symbolic Logic. *CRC Critical Reviews in Toxicology*. 11(4):279-332.
- Robeva, R. (2015), *Algebraic and Discrete Mathematical Methods for modern Biology*, Edited by Raina S. Robeva. Academic Press. Amsterdam and Boston (Massachusetts): Elsevier. \$106.25. xiii + 368 p.; ill.; index. ISBN: 978-0-12-801213-0.
- Shannon, CE. (1940). *A Symbol of Analysis of Relay and Switching Circuits*. Massachusetts Institute of Technology 1940
- Steffens HJ, Muehlmann K, Zoellner C. (2019). *Mathematik für Informatiker für Dummies*, Verlag: Wiley-VCH.
- Swerdlow, SH et al. (2008). *WHO Classification of Tumours of Haematopoietic and Lymphoid Tissues*, World Health Organization Classification of Tumours. 4th ed. Lyon: International Agency for Research on Cancer;
- Swerdlow SH et al. *WHO Classification of Tumours of Haematopoietic and Lymphoid Tissues*. Revised 4th ed. Lyon: International Agency for Research on Cancer; 2017.
- Takeuti G. (1987). *Proof Theory*. 2nd ed. Amsterdam, North Holland: Dover Publications.
- Varadan V, Anastassiou D. (2006). Inference of Disease-Related Molecular Logic from Systems-Based Microarray Analysis. *PLoS Computational Biology*. 2(6): 585-597. doi: 10.1371/journal.pcbi.0020068.eor
- Vivaldi F, (2014), *Mathematical Writing*, Springer
- Zugmaier G, Locatelli F. (2019). Application of Mathematical Logic for Immunophenotyping of B-Cell Precursor Acute Lymphoblastic Leukemia (BCP-ALL). *Biomedical Genetics and Genomics*. 4: 1-3. doi:10.15761/bgg.1000148
- Zugmaier G, Locatelli F. (2021). Application of Mathematical Logic for Cytogenetic Definition and Risk Stratification of B-Cell Precursor Acute Lymphoblastic Leukemia (BCP-ALL). *Medical Research Archives*. 9(2):1-8.
- Zugmaier G, Kerkmann S, Locatelli F. (2023). Application of Boolean Algebra for Definition of Myeloid, *Medical Research Archives, Neoplasms*, <https://doi.org/10.18103/mra.v11i1.3456>
- Gerhard Zugmaier, (2024), *Boolean Algebra for Laboratory Diagnostics in Medicine*, *J Clinical Research and Reports*, 16(2); DOI:10.31579/2690-1919/381
- ZUGMAIER, Gerhard; LOCATELLI, Franco. *Boolean Algebra (Mathematical Logic) for Grading of Toxicities Associated with Cellular Immune Therapy*. *Medical Research Archives*, [S.l.], v. 12, n. 10, oct. 2024. ISSN 2375-1924. Available at: <<https://esmed.org/MRA/mra/article/view/5765>>.



This work is licensed under Creative Commons Attribution 4.0 License

To Submit Your Article Click Here: **Submit Manuscript**

DOI: [10.31579/2690-1919/439](https://doi.org/10.31579/2690-1919/439)

**Ready to submit your research? Choose Auctores and benefit from:**

- fast, convenient online submission
- rigorous peer review by experienced research in your field
- rapid publication on acceptance
- authors retain copyrights
- unique DOI for all articles
- immediate, unrestricted online access

At Auctores, research is always in progress.

Learn more <https://www.auctoresonline.org/journals/journal-of-clinical-research-and-reports>